

Summary of COSC229 - Algorithms

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The topics covered are given in the following with time complexities.

1. Data structures

- 1.1 Binary search trees --- $O(n \log n)$ average for n insertions
- 1.2 AVL trees --- $O(n \log n)$ worst case for n insertions
- 1.3 Splay trees --- $O(n \log n)$ worst case for n insertions
- 1.4 2-3 trees --- $O(n \log n)$ worst case for n insertions
- 1.5 Heaps --- $O(n)$ for n insertions and $O(\log n)$ for delete-min
- 1.6 Binomial queues --- $O(\log n)$ for delete-min and $O(\log n)$ for meld

2. Sorting

- 2.1 Bubble sort --- $O(n^2)$
- 2.2 Minimum selection sort --- $O(n^2)$
- 2.3 Insertion sort --- $O(n^2)$
- 2.3 Heap sort --- $O(n \log n)$ worst case
- 2.4 Quick sort --- $O(n \log n)$ average
- 2.5 Merge sort --- $O(n \log n)$ worst case
- 2.6 Radix sort --- $O(dn)$ where d is number of digits

3. Graph algorithms

- 3.1 Basic definitions
- 3.2 Depth-first search --- $O(m + n)$
- 3.2 Breadth-first search --- $O(m + n)$
- 3.3 Tarjan's algorithm for strongly connected components -- $O(m+n)$
- 3.4 Dijkstra's algorithm for the single source shortest path problem -- $O(n^2)$
with heap -- $O(m \log n)$
- 3.5 Warshall's algorithm for reflexive-transitive closure --- $O(n^3)$
- 3.6 Floyd's algorithm for the all pairs shortest path problem --- $O(n^3)$
- 3.7 Kruskal's algorithm for the minimum cost spanning tree --- $O(m \log n)$
- 3.8 Prim's algorithm for the same problem --- $O(m \log n)$

4. Pattern matching

- 4.1 Naive algorithm --- $O(mn)$
- 4.2 KMP algorithm --- $O(m + n)$
- 4.3 Boyer-Moore algorithm --- $O(n/m)$ average
- 4.4 Bird's algorithm for two-dimensional pattern matching --- $O(m^2 + n^2)$

5. Computational geometry

- 5.1 Intersection of line segments --- $O(1)$
- 5.2 Interior point in a polygon --- $O(n)$
- 5.3 Naive algorithm for convex hull --- $O(n^2)$
- 5.4 Graham's algorithm for convex hull --- $O(n \log n)$
- 4.5 Lee's algorithm for Voronoi diagram --- $O(n \log n)$

6. Semi-numerical algorithms

6.1 Basics from number theory

6.2 Horner's algorithm for polynomial evaluation --- $O(n)$

6.3 Repeated squaring for exponentiation --- $O(m)$ where exponent is m bit number

6.4 Theory of Fibonacci numbers --- $O(\log n)$ for the n -th Fibonacci number

6.5 Euclidean algorithm for greatest common divisors --- $O(kD(k))$ where a and b are k bit numbers and $D(k)$ is the time for division

6.6 Euclidean algorithm for multiplicative inverses

6.7 Analysis of Euclidean algorithm

6.8 Discrete Fourier transform --- $O(n^2)$ by naive method and $O(n \log n)$ by FFT

6.9 Convolution --- $O(n^2)$ by naive method and $O(n \log n)$ by FFT

6.10 How to multiply polynomials fast --- (n^2) by naive method and $O(n \log n)$ by FFT

6.11 How to multiply multiple precision numbers fast --- $O(n^2)$ by naive method and $O(n \log n)$ by FFT