

COSC329 Tutorials on Combinatorial Generation

- (1) Make an algorithm for generating binary strings in reverse lexicographic order.
- (2) Make an algorithm for generating ternary strings in lexicographic order.
- (3) Draw the lexicographic tree of ternary strings of length 3. There are 27 leaves corresponding to the strings. Two strings 212 and 213 share the same path 21, etc.
- (4) Make a recursive algorithm for generating ternary strings with one change from string to string. Hint: Follow the algorithm for the binary reflected Gray code.
- (5) Make the twisted lexicotree for the above set of strings.
- (6) Convert the above algorithm into an iterative one.
- (7) Make an algorithm for generating permutations in reverse lexicographic order.
- (8) In Johnson's algorithm, n moves most frequently, $n-1$ moves next most frequently, ..., etc. Convert the algorithm so that 1 moves most frequently, 2 moves next most frequently, ..., etc.
- (9) Prove that the last permutation by Johnson's algorithm is $2\ 1\ 3\ 4\ \dots\ n$
- (10) A meta program is one that generate a nested loop structure such as Algorithm 9. Make such a meta program and run it. As a result you have a generated program. Run it and confirm you can generate combinations with an output statement. Compare the time with the recursive one for a large n and r . Remove the output statement for a large experiment..
- (11) Make a recursive algorithm that generates parenthesis strings in reverse lexicographic order.
- (12) Draw all binary trees with 4 internal nodes and confirm the number is 14. Give the correspondence between the parenthesis strings and the trees.
- (13) Draw all the diagonals of a polygon with $(n+2)$ vertices. The number is the n -th Catalan number. Confirm this with $n=4$. Give the correspondence between parenthesis strings and the diagonals.

Example with $n=3$. Originate a parenthesis string from 0. If you do not draw diagonal from 0 any more, go to 1, etc. In the second figure, we embrace a polygon of $n=4$.

